

# Sequential Modeling of Parity Progression Ratio in Sub-Saharan Africa\*

Gebrenegus Ghilagaber<sup>†</sup> and Paraskevi Peristera<sup>‡</sup>

## 1 Sequential Modeling of Parity Progression

Since the actual family size decision process requires successful completion of the prior level (parity) for passage into the subsequent one, a sequential decision model accurately reflects the real decision process (Yamaguchi & Ferguson, 1995; Upchurch, Lillard, & Panis, 2002). The model of family size decision used in this paper specifies the propensity of progressing to successively higher parity levels, conditional on having completed the next lower parity – a discrete sequential choice model. Apart from measured covariates, the sequential probabilities may depend on individual and decision varying covariates and unobserved heterogeneity in the propensity to continue to the next parity.

As the reasons to have a second child may differ from those to have a third child, we allow the effects on the transition propensities to vary between these two transitions (first to second, second to third). Thus, there are up to two sequential choices of whether to continue to the next level ( $s = 1, 2$ ), each conditional on having continued to the previous level. Here,  $s = 1$  corresponds to transition from 1 to 2 children, and  $s = 2$  corresponds to transition from 2 to 3 children.

We use a multilevel sequential probit model of individual-family (mother) choice. Family  $i$  progresses from having completed parity  $s$  to complete the

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<sup>†</sup>Department of Statistics, Stockholm University, Sweden. Gebre@stat.su.se

<sup>‡</sup>Stress Research Institute, Stockholm University, Sweden. Paraskevi.Peristera@su.se

next parity  $s + 1$  if its propensity to continue is positive.  $I_s > 0$ . The propensity of mother (family)  $i$  progressing is thus determined by the probit index function

$$I_{i(s)} = \alpha_{0s} + \alpha'_{1s} X_{i(s)} + v_i + \theta_s \quad (1)$$

for  $s = 1, 2$ . where  $X_s$  is a vector of exogenous covariates affecting family size decisions.  $\alpha_{0s}$  and  $\alpha_{1s}$  are decision specific intercepts and coefficients, respectively.  $v_i$  is a residual term capturing family level unobserved heterogeneity (shared-frailty) that may affect all levels of decision on family size, and  $\theta_s$  is a decision specific stochastic element (normalized to  $\theta_s = 1$ , for all  $s$ ). Each is assumed to be normally distributed:

$$v \sim N(0, \sigma_v^2). \quad \theta_s \sim N(0, 1).$$

The model also allows parameters to vary across decisions (hence the  $s$  subscript on the parameter vector  $\alpha$ ). In other words, we will estimate two intercepts and two sets of coefficient estimates, one set for transition to second child, and another set for transition from second to third.

Table 4 about here

In Table 4, we report results from fitting nested sequential probit models in which we allow the effects to vary across decision levels. The results in model M0 (when no covariates have been included) show that the most common transition is from single parity (one child) to parity 2 (2 children). We also note that women with higher IQ (in M1) have lower propensities to increase family size from two to three. However, any maternal IQ effect disappears once more variables are entered (in M4 and M5). Hispanic women have higher propensities of increasing family size from two to three (in M2), whereas Black women have lower propensities to have a second child, but higher propensities to have a third child (in M2). The higher propensity of having a third child disappears when mother's age at the birth of first child is entered. Women who were older at the birth of their first child (in M3) have lower propensities to increase family size, whereas those with higher incomes (in M4) have higher propensities. Finally, women with no college education (in M5) have a lower propensity to have a third child compared to those with some college, when all variables are included in the model.

Fertility studies generally find negative (or no) relationships between socioeconomic status indicators and family size in Western countries (e.g. Lawson and Mace, 2010). Our analyses, although restricted to families with at

most three children. show some positive effects of income and education when we control for maternal IQ, maternal race, and maternal age of first child. These results partly support findings of Weeden et al. (2006) who reported that male income (or income of spouse of female) may have a positive effect on family size.

## 2 Preliminary Results

Table 1: Estimated effects on log-odds of transition to various parities across covariates: Eritrea

		Transition to parity						
Covariate	Levels	1	2	3	4	5	6	7+
Moth Educ	Primary	0.374	-0.097	-0.078	-0.125	-0.021	-0.294	0.280
	Secondary+	0.793	-0.099	-0.414	-0.284	-0.507	-0.585	-0.392
Residence	Rural	0.196	0.447	0.339	0.114	-0.027	-0.368	0.144
Birth Cohort	1971-75	1.626	1.810	1.721	<i>20.181</i>	<i>Ref</i>	<i>Ref</i>	-
	1966-70	2.855	3.369	3.359	<i>21.252</i>	<i>1.456</i>	<i>20.884</i>	<i>Ref</i>
	1961-65	3.699	4.550	4.417	<i>22.464</i>	<i>2.413</i>	<i>21.686</i>	<i>0.782</i>
	1956-60	4.301	5.274	5.216	<i>23.346</i>	<i>3.291</i>	<i>22.575</i>	<i>2.032</i>
	1951-55	4.079	5.851	5.448	<i>23.841</i>	<i>4.226</i>	<i>22.951</i>	<i>2.569</i>
	1946-50	5.080	5.486	5.533	<i>23.777</i>	<i>4.065</i>	<i>23.342</i>	<i>2.831</i>
AgeMar	20-24	-1.336	-1.280	-0.863	-0.891	-0.539	-0.959	-0.684
	25+	-2.520	-2.547	-1.988	-1.475	-1.644	-1.688	-1.957

Table 2: Estimated effects on log-odds of transition to various parities across covariates: Ghana

		Transition to parity						
Covariate	Levels	1	2	3	4	5	6	7+
Moth Educ	Primary	0.132	-0.054	-0.406	-0.022	-0.022	0.021	-0.175
	Secondary+	-0.179	-0.566	-0.936	-0.624	-0.624	-0.716	-0.385
Residence	Rural	0.570	0.446	0.524	0.692	0.692	0.438	0.667
Birth Cohort	1971-75	1.632	2.487	19.990	Ref	Ref	Ref	-
	1966-70	3.495	4.194	21.611	0.747	0.747	20.740	Ref
	1961-65	4.389	5.620	23.200	2.078	2.078	21.350	1.050
	1956-60	5.367	6.347	24.205	2.909	2.909	22.440	1.876
	1951-55	6.410	6.716	24.547	3.633	3.633	23.078	2.765
	1946-50	5.610	7.129	24.971	3.814	3.814	23.042	3.108
AgeMar	20-24	-2.021	-1.255	-1.287	-0.953	-0.953	-0.737	-0.749
	25+	-3.840	-2.677	-2.399	-1.736	-1.736	-1.122	-1.717

Table 3: Estimated effects on log-odds of transition to various parities across covariates: Kenya

		Transition to parity						
Covariate	Levels	1	2	3	4	5	6	7+
Moth Educ	Primary	0.774	-0.082	-0.088	-0.191	-0.160	-0.323	-0.321
	Secondary+	0.902	-0.464	-0.550	-0.887	-0.548	-0.626	-1.062
Residence	Rural	0.671	0.462	0.697	1.012	1.197	0.744	0.362
Birth Cohort	1971-75	1.845	1.663	3.499	19.456	Ref	Ref	Ref
	1966-70	3.677	3.805	4.931	21.275	0.638	0.824	20.522
	1961-65	4.482	5.457	6.527	22.463	1.668	1.778	21.413
	1956-60	3.995	5.709	7.336	23.261	2.543	2.733	22.261
	1951-55	4.636	5.857	7.898	23.483	3.014	3.584	22.892
	1946-50	4.294	5.539	7.815	24.147	3.696	3.848	23.239
AgeMar	20-24	-1.712	-1.563	-1.536	-1.028	-1.010	-1.061	-0.493
	25+	-3.204	-3.048	-2.352	-2.428	-1.608	-1.550	-3.910

Table 4: Estimated effects on log-odds of **transition to various parities** across covariates and

		Transition to parity 1			Transition to parity 2			Transition
<b>Covariate</b>	<b>Levels</b>	<b>Eritrea</b>	<b>Ghana</b>	<b>Kenya</b>	<b>Eritrea</b>	<b>Ghana</b>	<b>Kenya</b>	<b>Eritrea</b>
Moth Educ	Primary	0.374	0.132	0.774	-0.097	-0.054	-0.082	-0.078
	Secondary+	0.793	-0.179	0.902	-0.099	-0.566	-0.464	-0.414
Residence	Rural	0.196	0.570	0.671	0.447	0.446	0.462	0.339
Age at Int	20-24	1.626	1.632	1.845	1.810	2.487	1.663	1.721
	25-29	2.855	3.495	3.677	3.369	4.194	3.805	3.359
	30-34	3.699	4.389	4.482	4.550	5.620	5.457	4.417
	35-39	4.301	5.367	3.995	5.274	6.347	5.709	5.216
	40-44	4.079	6.410	4.636	5.851	6.716	5.857	5.448
	45-49	5.080	5.610	4.294	5.486	7.129	5.539	5.533
AgeMar	20-24	-1.336	-2.021	-1.712	-1.280	-1.255	-1.563	-0.863
	25+	-2.520	-3.840	-3.204	-2.547	-2.677	-3.048	-1.988

Table 5: Estimated effects on log-odds of **transition parities** across covariates and countries

		Transition to parity 1			Transition to parity 2		
<b>Covariate</b>	<b>Levels</b>	<b>Eritrea</b>	<b>Ghana</b>	<b>Kenya</b>	<b>Eritrea</b>	<b>Ghana</b>	<b>Kenya</b>
<b>Highest Educ Level</b>	<i>Primary</i>	0.374	0.132	0.774	-0.097	-0.054	-0.082
	<i>Secondary+</i>	0.793	-0.179	0.902	-0.099	-0.566	-0.464
<b>Residence</b>	<i>Rural</i>	0.196	0.570	0.671	0.447	0.446	0.462
<b>Age at Interview</b>	<i>20-24</i>	1.626	1.632	1.845	1.810	2.487	1.663
	<i>25-29</i>	2.855	3.495	3.677	3.369	4.194	3.805
	<i>30-34</i>	3.699	4.389	4.482	4.550	5.620	5.457
	<i>35-39</i>	4.301	5.367	3.995	5.274	6.347	5.709
	<i>40-44</i>	4.079	6.410	4.636	5.851	6.716	5.857
	<i>45-49</i>	5.080	5.610	4.294	5.486	7.129	5.539
<b>Age at Marriage</b>	<i>20-24</i>	-1.336	-2.021	-1.712	-1.280	-1.255	-1.563
	<i>25+</i>	-2.520	-3.840	-3.204	-2.547	-2.677	-3.048

